I. Kolmogorov Complexity
Five key ideas

• Digital encoding
• Counting bits
• Compression
• Programs
• Conditional complexity
1. Digital encoding

Hello!

72 101 108 108 111 33

01001000 01100101 01101100 01101100 01101111 00100001
1. Digital encoding
1. Digital encoding
1. Digital encoding
2. Counting bits

You Got the Right One, Uh-Huh

232 bits
2. Counting bits

Thou still unravished bride of quietness,
Thou foster-child of silence and slow time,
Sylvan historian, who canst thus express
A flowery tale more sweetly than our rhyme

...“Beauty is truth, truth beauty,—that is all
Ye know on earth, and all ye need to know”
3. Compression

Happy_birthday_to_you←
Happy_birthday_to_you←
Happy_birthday_dear_X←
Happy_birthday_to_you←

704 bits
3. Compression

1: Happy_birthday
2: *1_to_you*

*2*2*1_dear_X*2

368 bits
4. Programs

\[ K(w) = \min l(p): p() = w \]
4. Programs

XXXXXXXXXXXX (10 Xs)  80 bits

XXXXXXXXXX...XXXXXXXX (100 Xs)  800 bits

XXXXXXXXXX...XXXXXXXXXX (1000 Xs)  8000 bits

XXXXXXXXXX...XXXXXXXXXXXXXX (10000 Xs)  80000 bits
4. Programs

XXXXXX (10 Xs) 80 bits
for($i=0;$i<10;$i++){print"X"} 240 bits

XXXXX...XXXXX (100 Xs) 800 bits
for($i=0;$i<100;$i++){print"X"} 248 bits

XXXXX...XXXXXXX (1000 Xs) 8000 bits
for($i=0;$i<1000;$i++){print"X"} 256 bits

XXXXX...XXXXXXXX (10000 Xs) 80000 bits
for($i=0;$i<10000;$i++){print"X"} 264 bits
5. Conditional complexity
5. Conditional complexity

\[ K(x|\gamma) = \min l(p): p(\gamma) = x \]
5. Conditional complexity

\[ K(\cdot) = \text{high} \]
\[ K(\cdot \mid \cdot) = \text{medium} \]
\[ K(\cdot) - K(\cdot \mid \cdot) = \text{high} \]
\[ K(\cdot \mid \cdot) = \text{high} \]
\[ K(\cdot) - K(\cdot \mid \cdot) = \text{low} \]
II. Copyright
An unworkable proposal

• Use $K(x)$ to measure expression

• Use $K(x|y)$ to measure similarity

• *Virtue*: common metric among different types of work (poems, movies, songs, etc.)

• *Virtue*: filtration of unoriginal similarity
Objections

• Objection: $K$ is uncomputable
• Objection: $K$ ignores psychology and aesthetics
A revised proposal

• $K$ cannot show that a work is expressive, but it can show that a work is not expressive

• Use $K$ as a first step to ask whether a work is complex enough to be potentially copyrightable, or whether two works have enough similarity for infringement

• Second step: fact-finding about ordinary lay audience’s reactions

• Maybe the Ninth Circuit has it right!